[Total No. of Questions - 5] [Total No. of Pri\ d Pages - 2] (2126)

M. Tech 1st Semester Examination

Advanced Fluid Mechanics

WRE-101

Time: 3 Hours

Max. Marks: 100

The candidates shall limit their answers precisely within the answerbook (40 pages) issued to them and no supplementary/continuation sheet will be issued.

Note: Attempt all questions. All questions carry equal marks.

- 1. (a) What is the Lagrangian description of the fluid motion?

 How does it differ from Eulerian description? (12)
 - (b) Consider the following steady, two dimensional velocity fields:

(i)
$$\vec{V} = (u, v) = [a^2 - (b - cx)^2]\vec{i} + (-2cby + 2c^2xy)\vec{j}$$

(ii)
$$\vec{V} = (u, v) = (0.5 + 1.2x)\vec{i} + (-2.0 - 1.2y)\vec{j}$$
 (8)

- 2. (a) Describe acceleration of an ideal fluid element in Cartesian and cylindrical polar coordinates, given $\overline{q} = \overline{u}_i + \overline{v}_j + \overline{w}_k$ as velocity vector, where u, v and w are functions of x, y, z and t, where $u = x_i + 2y_j + 3z_k$; $v = 2x_i + 3y_j + 4z_k$; $w = 3x_i + 4y_j + 5z_k$. (10)
 - (b) Determine the resultant of an uniform flow of an ideal fluid superimposed on a doublet. Determine the relationship between this flow and that of an ideal fluid past a circular cylinder. (10)
- (a) Describe a normal shock on h-s diagram. Obtain the governing relation for a normal shock to evaluate Mach number M₂ downstream of a normal shock for a given upstream condition of M₁. (12)

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(b) How do you estimate the effects of a moving shock wave with the help of relative velocity method (i) when the observer is stationary and (ii) when the observer is located on the shock wave itself.

(8)

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- (a) Derive the Navier-Stokes equation of motion for an incompressible viscous fluid in Cartesian coordinate system. (10)
 - (b) What do you understand by an exact solution of Navier-Stokes equation? Discuss briefly with suitable example of a fully developed in a pipe/ between parallel plates. (10)
- 5. (a) Explain the significance of divergence of velocity and substantial derivative. How substantial derivative different than derivative in differential calculus? (12)
 - (b) Explain any two types of errors encountered in numerical methods and indicate how the error occurs? (8)